# ECE317 HW #9

## **Problem 1:**

Determine the type of the following unity-feedback systems for which the forward-path transfer functions are given:

(a) 
$$G(s) = \frac{K}{(1+s)(1+10s)(1+20s)}$$
 (b)  $G(s) = \frac{10e^{-0.2s}}{(1+s)(1+10s)(1+20s)}$   
(c)  $G(s) = \frac{10(s+1)}{s(s+5)(s+6)}$  (d)  $G(s) = \frac{100(s-1)}{s^2(s+5)(s+6)^2}$   
(e)  $G(s) = \frac{10(s+1)}{s^2(s+5)(s+6)}$  (f)  $G(s) = \frac{100}{100}$ 

(g) 
$$G(s) = \frac{5(s+2)}{s^2(s+4)}$$
 (h)  $G(s) = \frac{8(s+1)}{(s^2+2s+3)(s+1)}$ 

## **Problem 2:**

Determine the step, ramp and parabolic error constants of the following unity-feedback control systems. The forward-path transfer functions are given by:

(a) 
$$G(s) = \frac{1000}{(1+0.1s)(1+10s)}$$
 (b)  $G(s) = \frac{100}{s(s^2+10s+100)}$   
(c)  $G(s) = \frac{K}{s(1+0.1s)(1+0.5s)}$  (d)  $G(s) = \frac{100}{s^2(s^2+10s+100)}$   
(e)  $G(s) = \frac{1000}{s(s+10)(s+100)}$  (f)  $G(s) = \frac{K(1+2s)(1+4s)}{s^2(s^2+s+1)}$ 

## **Problem 3:**

For the unity-feedback control systems described in Problem 2, determine the steady-state error for a unit-step,  $u_s(t)$ , unit-ramp,  $tu_s(t)$ , and parabolic input  $\left(\frac{t^2}{2}\right)u_s(t)$ . Check the stability of the system before applying the final-value theorem.

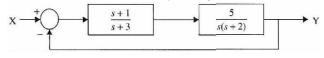
#### **Problem 4:**

The following transfer functions are given for a single-loop non-unity-feedback control system. Determine the steady errors for a unit-step,  $u_s(t)$ , unit-ramp,  $tu_s(t)$ , and parabolic input,  $\left(\frac{t^2}{2}\right)u_s(t)$ .

(a) 
$$G(s) = \frac{1}{(s^2 + s + 2)}$$
  $H(s) = \frac{1}{(s + 1)}$   
(b)  $G(s) = \frac{1}{s(s + 5)}$   $H(s) = 5$   
(c)  $G(s) = \frac{1}{s^2(s + 10)}$   $H(s) = \frac{s + 1}{s + 5}$   
(d)  $G(s) = \frac{1}{s^2(s + 12)}$   $H(s) = 5(s + 2)$ 

# Problem 5:

Find the position, velocity and acceleration constants for the system given below.



#### Problem 6:

For the system of Problem 5, find the steady-state error for (a) a unit-step,  $u_s(t)$ , (b) a unit-ramp,  $tu_s(t)$ , and (c) a unit parabolic input,  $\left(\frac{t^2}{2}\right)u_s(t)$ .