## ECE317

## HW \#3

Do the selected problems listed next from the following two attached pages.
Probs. 2a, 4, a, b, d and f of problems 8,17 and $18, \quad 20 \mathrm{a}, \quad 23 \mathrm{a}$ and $\mathrm{c}, \quad 24$

State Space
SS
20. What three pieces of information must be given in order to solve for the output response of a system using state-space techniques?
21. How can the poles of a system be found from the state equations?

## Problems

1. Derive the output responses for all parts of Figure 4.7. [Section: 4.4]
2. Find the output response, $c(t)$, for each of the systems shown in Figure P4.1. Also find the time constant, rise time, and settling time for each case. [Sections: 4.2, 4.3]


FIGURE P4.1
3. Plot the step responses for Problem 2 using MATLAB.
4. Find the capacitor voltage in the network shown in Figure P4.2 if the switch closes at $t=0$. Assume zero initial conditions. Also find the time constant, rise time, and settling time for the capacitor voltage. [Sections: 4.2, 4.3]


FIGURE P4.2
5. Plot the step response for

MATLAB
Problem 4 using MATLAB. From ML your plots, find the time constant, rise time, and settling time.
6. For the system shown in Figure P4.3, (a) find an equation that relates settling time of the velocity of the mass to $M$; (b) find an equation that relates rise time of the velocity of the mass to M. [Sections: 4.2, 4.3]


FIGURE P4.3
7. Plot the step response for MATLAB Problem 6 using MATLAB. From your ML plots, find the time constant, rise time, and settling time. Use $M=1$ and $M=2$.
8. For each of the transfer functions shown below, find the locations of the poles and zeros, plot them on the $s$-plane, and then write an expression for the general form of the step response without solving for the inverse Laplace transform. State the nature of each response (overdamped, underdamped, and so on). [Sections: 4.3, 4.4]
a. $T(s)=\frac{2}{s+2}$
b. $T(s)=\frac{5}{(s+3)(s+6)}$
c. $T(s)=\frac{10(s+7)}{(s+10)(s+20)}$
d. $T(s)=\frac{20}{s^{2}+6 s+144}$
e. $T(s)=\frac{s+2}{s^{2}+9}$
f. $T(s)=\frac{(s+5)}{(s+10)^{2}}$
9. Use MATLAB to find the poles of MATLAB
[Section: 4.2] ML

$$
T(s)=\frac{s^{2}+2 s+2}{s^{4}+6 s^{3}+4 s^{2}+7 s+2}
$$

10. Find the transfer function and poles of the system represented in state space here. [Section: 4.10]

$$
\begin{aligned}
& \dot{\mathbf{x}}=\left[\begin{array}{rrr}
3 & -4 & 2 \\
-2 & 0 & 1 \\
4 & 7 & -5
\end{array}\right] \mathbf{x}+\left[\begin{array}{r}
-1 \\
-2 \\
3
\end{array}\right] u(t) \\
& y=\left[\begin{array}{lll}
1 & 7 & 1
\end{array}\right] \mathbf{x} ; \mathbf{x}(0)=\left[\begin{array}{l}
0 \\
0 \\
0
\end{array}\right]
\end{aligned}
$$

11. Repeat Problem 10 using MATLAB. matlab [Section: 4.10]
12. Write the general form of the capacitor voltage for the electrical network shown in Figure P4.4. [Section: 4.4]


## FIGURE P4.4

13. Use MATLAB to plot the capacitor MATLAB voltage in Problem 12. ML [Section: 4.4]
14. Solve for $x(t)$ in the system shown in Figure P4.5 if $f(t)$ is a unit step. [Section: 4.4]


FIGURE P4.5
15. The system shown in Figure P 4.6 has a unit step input. Find the output response as a function of time. Assume the system is underdamped. Notice that the result will be Eq. (4.28). [Section: 4.6]


## FIGURE P4.6

16. Derive the relationship for damping ratio as a function of percent overshoot, Eq. (4.39). [Section: 4.6]
17. Calculate the exact response of each system of Problem 8 using Laplace transform techniques, and
compare the results to those obtained in that problem. [Sections: 4.3, 4.4]
18. Find the damping ratio and natural frequency for each second-order system of Problem 8 and show that the value of the damping ratio conforms to the type of response (underdamped, overdamped, and so on) predicted in that problem. [Section: 4.5]
19. A system has a damping ratio of 0.15 , a natural frequency of $20 \mathrm{rad} / \mathrm{s}$, and a dc gain of 1 . Use inverse Laplace transforms to find an analytic expression of the response of the system to a unit-step input. [Section: 4.6]
20. For each of the second-order systems that follow, find $\zeta, \omega_{n}, T_{s}, T_{p}, T_{r}$, and $\% O S$. [Section: 4.6]
a. $T(s)=\frac{16}{s^{2}+3 s+16}$
b. $T(s)=\frac{0.04}{s^{2}+0.02 s+0.04}$
c. $T(s)=\frac{1.05 \times 10^{7}}{s^{2}+1.6 \times 10^{3} s+1.05 \times 10^{7}}$
21. Repeat Problem 20 using

MATLAB. Have the computer program estimate the given specifications and plot the step responses. Estimate the rise time from the plots. [Section: 4.6]
22. Use MATLAB's LTI Viewer and GUl Tool obtain settling time, peak time, GUIT rise time, and percent overshoot for each of the systems in Problem 20. [Section: 4.6]
23. For each pair of second-order system specifications that follow, find the location of the second-order pair of poles. [Section: 4.6]
a. $\% O S=12 \% ; T_{s}=0.6$ second
b. $\% O S=10 \% ; T_{p}=5$ seconds
c. $T_{s}=7$ seconds; $T_{p}=3$ seconds
24. Find the transfer function of a second-order system that yields a $15 \%$ overshoot and a settling time of 0.7 second. [Section: 4.6]
25. For the system shown in Figure P4.7, do the following: [Section: 4.6]
a. Find the transfer function $G(s)=X(s) / F(s)$.
b. Find $\zeta, \omega_{n}, \% O S, T_{s}, T_{p}, T_{r}$, and $C_{\text {final }}$ for a unit-step input.

